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RESEARCH PAPER

Enhancing Cable-Stayed Bridge Structural Health Assessment Using Phase Space Trajectory and Load Pattern Variability

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ABSTRACT: A novel approach for assessing the structural health of cables in cable-stayed bridges, under varying load patterns, was presented. The method aimed to evaluate cable conditions by utilizing phase space analysis while minimizing traffic disruptions and reducing the necessity for extensive sensor deployment. Through comprehensive numerical investigations on the Manavgat cable-stayed bridge, the efficacy of the proposed method was demonstrated. For this purpose, the time-domain responses of the deck were utilized. The combination of Change in Phase Space Topology (CPST) and Mahalanobis Distance (MD) indices was applied to detect cable damage by discerning nuanced deviations in phase space trajectories. The results revealed that both the MD and CPST indices exhibited impressive accuracy in identifying damage severity and location. To emphasize the robustness of the phase space-based damage detection method, a comparative analysis between the CPST and modal parameters was conducted. At the 10% damage level, the accuracy of CPST increased by 84.5% compared to the first mode frequency of the structure in load state 1. It highlighted the high sensitivity of CPST in cable damage detection.

Keywords: Cable-Stayed Bridge, Structural Health Monitoring, Phase Space Method, Damage Detection, Time Domain Responses.

1. Introduction

A cable-stayed bridge is a type of bridge where the deck is supported by a system of cables connected to one or more towers. These cables extend directly from the tower to the deck, forming a pattern that resembles a fan or a series of parallel lines. Cable-stayed bridges are widely used for medium to long spans, ranging from 200 m to well over 1,000 m. Cable-stayed bridges, noted

for their distinctive appearance, structural efficacy, and ability to span significant distances without intermediate piers, are often located in regions where conventional suspension bridge construction is impractical due to geological or environmental constraints.

Stay cables, as the main load-bearing components of a bridge, typically account for approximately 25-30% of the total construction cost. Moreover, the cost of

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replacing cables can be nearly 3-4 times higher than that of new construction (He et al., 2022). As such, ensuring the health of cables throughout the lifespan of the structure and assessing their operational efficiency are paramount concerns, especially for both existing and newly constructed cable-stayed bridges. practice of Structural Health Monitoring (SHM) for bridges involves continuously collecting and analyzing data about the condition throughout bridge's operational lifespan. The goal of SHM is to quantify any and potential deterioration that may occur during service, while also providing relevant recommendations for maintenance and oversight of the structure. SHM systems typically utilize various sensors, such as accelerometers. strain gauges, and displacement transducers, to capture the structural responses of the bridge to external forces, including traffic, wind, and seismic activity. After data collection, advanced algorithms are employed to analyze the data and identify changes in the structural dynamics of the bridge, including variations in natural frequencies, mode shapes, and damping ratios. This strategic approach enables the early detection of structural impairments, facilitating prompt rectification and maintenance. technique reduces the risk of catastrophic failures and extends the operational lifespan of the bridge. Furthermore, structural health monitoring helps optimize maintenance schedules and reduce maintenance costs by providing accurate insights into condition of the bridge (Saidin et al., 2023).

In essence, the core of SHM lies in identifying, locating, and quantifying damage through dynamic responses. This comprehensive methodology assessing and predicting damage at both local and global levels (Pamwani and Shelke, 2018). In the field of monitoring performance and ensuring the longevity of engineering structures, the implementation of SHM has provided invaluable insights over extended periods. Over

numerous numerical and experimental studies have explored the field of cablestayed bridge health monitoring. The assessment of bridge health and dynamic characteristics in most studies has typically been examined under various environmental conditions, moving loads, artificial vibrations, or stimuli such as earthquakes. Bakhshizadeh et al. (2023) investigated the impact of Multiple Support Excitations (MSE) on the dynamic response of large-span cable-stayed bridges to Various seismic hazards. identification methods, including mode shape curvature and modal strain energy techniques, were utilized for health monitoring to assess structural performance identify potential and damages (Bakhshizadeh and Sadeghi, 2023). Numerous researchers have directed their investigations toward ambient vibration (Bedon et al., 2016; Hong et al., 2012).

Prawin et al. (2020) introduced a diagnostic scheme for bridges with minimal measurements, considering environmental variations operational alongside measurement noise. Null subspace analysis was employed in the first stage to confirm the presence of damage using ambient vibration data through online monitoring. It was concluded from the investigations that the proposed approach was capable of detecting and localizing multiple, as well as damages under environmental conditions with very limited noise-contaminated measurements.

Vibration-based methods have played a central role in the field of structural health assessment. A prominent approach is the modal-based damage detection algorithm, which requires the automated identification continuous tracking of modal parameters for real-time analysis (Li et al., 2014). These methodologies have been comprehensive validated through computational modeling and empirical investigations. A notable study was the work by Saidin et al. (2023), which focused on structural health monitoring using a vibration-based approach for an Ultra-

(UHPC) High-Performance Concrete bridge. In this study, researchers extracted mode shapes, natural frequencies, and damping ratios to understand the modal characteristics of the bridge. parameters were then used to assess the bridge's performance and monitor its health over time. The main objective of this study was to highlight the effectiveness of SHM in detecting structural impairments and predicting the behavior of engineering Also, Vibration-based structures. methodologies are extensively utilized for estimating cable tension and evaluating the comprehensive health of cable structures.

Fatigue and corrosion have presented recurring challenges that can affect cables, leading to decreased stiffness and compromised force transmission.

Therefore, monitoring tension, as the primary indicator of cable health, is of paramount importance. This consideration arises from the relationship between cable tension, its strength, and stiffness. Cable tension can be determined using various methodologies, including direct force measurements, non-contact sensor or assessments of measurements, parameters like stress, strain, or natural frequency (Cheng et al., 2024; Fathali et al., 2020; Rinaldi et al., 2023; Yu, 2020). An illustrative example is the study conducted by Zarbaf et al. (2018), who utilized this technique to evaluate the cables of the Ironton-Russell Bridge. Their findings were subsequently compared with those obtained from lift-off tests. These approaches have utilized the natural frequencies, mechanical properties, and geometric features of cables to estimate tension. Jana et al. (2022) introduced a framework that utilized videobased measurements as multiple sensors to minimize estimation errors in real-time cable tension determination. Non-contact video-based sensing offered superior spatial resolution and lower costs compared to conventional sensors. The algorithm was implemented on the Fred-Hartman cablestayed bridge in Texas, demonstrating accurate tension estimation from videobased measurements. This showcased the significant potential of the framework in structural health monitoring. Damage detection methods under moving load can be categorized into two methods: the frequency domain method and the time domain method (He et al., 2017; Wu et al., 2017, 2019).

While frequency measurement provides high precision, it tends to offer a global perspective. It has posed challenges for local damage detection. Conversely, mode shape and its derivatives, such as modal curvature and modal flexibility, have theoretically shown sensitivity to damage.

However, they are often affected by measurement noise, compromising their reliability in practical civil structural health monitoring scenarios when displacement or acceleration data (Hong et al., 2012; Wu et al., 2017). In some investigations, Time Domain Responses (TDR) have proven to be effective tools for identifying localized damage. TDR-based methods directly identify damage from the output, bypassing the need for conversion into structural modal information. Zhang et al. (2020) introduced a rapid output-only technique for detecting damage in highway bridges under moving vehicles, relying on the fractal dimension of long-gauge FBG strain responses. The feasibility of both single and multiple damage scenarios was demonstrated through simulations and an indoor bridge-vehicle experiment. Additionally, model method's resistance to noise was assessed by adding a Signal-Noise Ratio (SNR) of 30 dB in the numerical simulation, and the impact of varying sensor quantities was investigated. In another study, Kordi and Mahmoudi (2022) presented a new method for detecting damage in truss bridges under moving loads. Damage was identified by comparing the displacement response curve shapes of the intact and damaged models with the axial force influence line curve shape. The results showed that the proposed method can accurately identify the damaged members. Cable-stayed bridges

renowned for their flexibility. In this structural configuration, the girder operates like a beam resting on a flexible foundation, while the cables provide flexible support from their anchoring points. The primary load paths across the bridge deck provide valuable insights into the condition of secondary structural elements, such as the stay cables. Nazarian et al. (2016) introduced a straightforward approach to recognizing damage in the cables of cablestayed bridges. This method involved monitoring variations in support reactions by analyzing shear forces acting upon deck components near the support locations. The researchers also proposed a technique to identify cables that have experienced partial or complete loss of tensile force, achieved by measuring strains along the bridge deck.

It is important to acknowledge that this technique may face challenges in accurately modeling geometric constraints boundary conditions, potentially resulting in inaccuracies. Displacements of the main beam and towers are key indicators of bridge performance, commonly tracked using Global Positioning System (GPS) sensors. For example, in long-span cablestayed bridges, these displacements are often measured statically during load testing before the bridge is opened to traffic. Although acceleration measurements can also provide displacement data, their precision is lower (Zhang et al., 2023).

Additionally, various factors such as temperature fluctuations, wind forces, and vehicular traffic impact the displacement of long-span bridges. Lei et al. (2023) proposed an approach involving the use of a one-dimensional residual convolutional autoencoder model to estimate displacement responses of a cable-stayed bridge under various loading conditions. To implement this approach, the researchers collected monitoring data from a cablestayed bridge, including comprehensive measurements of varied loads corresponding displacement responses.

Subsequently, temperature, wind, and vehicle load characteristics were used as

input variables, while the displacement responses at the mid-span of the main girder and the tops of the two pylons were used as output variables. The model underwent training and validation procedures using the collected monitoring data. It achieved an accuracy exceeding 95% in predicting a range of displacement responses associated with multiple critical loads, all used simultaneously as inputs. Within the field of civil engineering, phase space analysis has emerged as a valuable tool for damage detection. This methodology initially relies on strain history data, transforming time series data into a spatial domain, where even slight changes in parameters can propagate throughout the entire system. The Change in Phase Space Topology (CPST) index has been introduced as an immensely effective method, capable of increasing in value proportionally to the severity of damage, regardless of its location (Nie et al., 2012, 2013). Zhang et al. (2017) introduced a model-free method for detecting damage in bridge structures under moving loads, relying on changes in phase trajectory across multiple vibration measurements. The sensitivity and reliability of this approach were examined through numerical analysis of a simply supported beam structure. Experimental validation revealed that shear connection failures in a composite bridge structure model subjected to moving loads were effectively identified by the method. In multidimensional statistical analysis, the MD is another index that refers to a measure of distance on the scale of standard deviation between an observation and a reference sample. Like CPST, it has been introduced as a damage index in studies health monitoring related to Maesschalck et al., 2000; Pamwani and Shelke, 2018). The significant sensitivity of phase space analysis to damage has made it widely used in various studies on structural damage detection (Li et al., 2021; Paul et al., 2017; Peng et al., 2022; Tuttipongsawat et al., 2019). According to the studies, modal parameters such as natural frequency have shown limited sensitivity to local bridges. damages in Additionally, vibration-based methods for detecting damage have often disrupted traffic flow or required complete bridge closures if necessary. In examining the structure's behavior in the frequency domain, time is also dedicated to converting responses from the time domain to the frequency domain, resulting in a large volume of data. In the literature review on moving loads, the assessment of structural health has typically been conducted using a single type of load pattern. In this article, a novel approach was introduced for tracking cable health in cable-stayed bridges subjected to various load patterns. The approach included a comprehensive examination of phase space reconstruction and damage-sensitive indexes. This method observed how the structure behaves over time with minimal traffic disruptions or bridge closures, achieved by applying a specific load. The need for multiple and costly sensors was removed throughout the bridge deck using sensors or non-contact displacement methods. In this study, a rapid method was provided for early damage detection in cable-stayed bridges by using only one type of response. The research conducted in the realm of damage detection using phase portraits has often focused on structures such as frames, buildings, and highway bridges. In this research, the efficacy of phase space analysis was assessed on a cable-stayed bridge using both the change phase space topology and Mahalanobis distance indexes. A cablestayed bridge located in Turkey, featuring a steel pylon, a composite deck, and 28 steel investigated. cables, was Numerous damage scenarios, encompassing distinct load patterns and speeds, were evaluated.

The proposed method involved reconstructing the deck's displacement at the cable connection points in the phase space and subsequently examining the resulting damage indexes.

2. Methods

2.1. Phase Space Reconstruction

Phase space analysis is a novel method for structural damage detection. The method demonstrates exceptional sensitivity to damage because it magnifies changes in time-domain responses by converting them into a spatial domain. In phase space, each variable represents a distinct dimension in a multi-dimensional space, indicating that any change in one parameter will propagate throughout the entire system. Dynamic systems can be defined by their measured time-series responses in phase space. The phase space can be reconstructed using multiple variables or the time series of a single measured variable, incorporating parameters such as time lag(T) and embedding dimension (d) (Takens, 1981).

Given a time series measurement denoted as x(i) with N data points (where i = 1, ..., N), the reconstruction of the phase space can be formulated as follows (Tuttipongsawat et al., 2019):

$$X(n) = [x(n).x(n+T)....x(n + (d-1)T)]$$
 (1)

Each dimension can be expressed as:

$$x(n) = [x(1).x(2)....x(N - (d - 1)T)]$$

$$x(n + T) = [x(1 + T).x(2 + T)....x(N - (d - 2)T)]$$
...
$$x(n + (d - 1)T) = [x(1 + (d - 1)T).x(2 + (d - 1)T)....x(N)]$$
(2)

The set of all dimensions plotted is called the phase space topology. The geometry of the phase trajectory is closely related to the behavior of the structure. Any damage to the structure leads to changes in responses, which are accurately depicted in the topology of the phase space. By assessing the dissimilarity of the topology when damage occurs, it is possible to detect the presence of damage. Selecting an appropriate time lag is crucial during the reconstruction process.

The time lag can be determined using methods such as the Autocorrelation Function and the Average Mutual Information Function (AMIF). Typically, the lag for reconstruction is chosen as the time corresponding to the first zero crossing of the Autocorrelation Function or the first minimum of the AMIF (Abarbanel, 2012; Jiang et al., 2010). Similarly, the optimal choice of the embedding dimension (d) is essential in the reconstruction process.

Prominent techniques used to determine the appropriate embedding dimension include Singular System Analysis (SSA) and False Nearest Neighbor (FNN) methods (Broomhead and King, 1986; Nichols, 2003; Rhodes and Morari, 1997). In this study, the Average Mutual Information Function and False Nearest Neighbor methods were employed to determine the time lag and embedding dimension, respectively.

2.2. Damage Sensitive Feature

In this study, the relationship between the geometry of the phase space trajectory and the dynamic response of the structure was discussed. As damage gradually occurs, discernible changes are triggered within the dynamic response, which are distinctly reflected in the topology of the phase space. Two damage indices were used for damage detection in cable-stayed bridges: The CPST and the MD between phase space trajectories. These indices have been proposed as valuable tools for evaluating the health of the structure using phase space analysis (Nichols, 2003).

2.2.1. Change in Phase Space Topology (CPST)

The CPST index concept aims to difference between the measure the predicted damage case and the actual damage case. Assume X(n) and Y(n) are phase space reconstructions of a healthy case and a damaged case, respectively. The calculation concept is illustrated in Figure 1 (Tuttipongsawat et al., 2019). To begin, a fiducial point Y(r) at time index r from the damage case is selected, and mapped on the healthy case. By minimizing the Euclidean norm, the nearest p neighbors of this fiducial point are chosen in the healthy case (Nie et al., 2013; Pamwani and Shelke, 2018; Tuttipongsawat et al., 2019):

$$NN(n_j): \min ||X(n_j) - Y(r)||. \quad j$$

$$= 1....p$$
(3)

where P: denotes the total number of neighborhood points, and the operator $\|\cdot\|$: calculates the Euclidean norm. The set of nearest neighbor points to the fiducial point Y(r): is denoted as NN. These selected neighborhood points are used to quantify the dissimilarity between the healthy and damaged cases. The predicted damage case at the 's' time step can be computed using Eq. (4) (Nie et al., 2013; Pamwani and Shelke, 2018; Tuttipongsawat et al., 2019).

$$\overset{\mathbb{I}}{Y}(r+s) = \frac{1}{P} \sum_{i=1}^{P} X(n_j + s). \quad j = 1, \dots, p$$
(4)

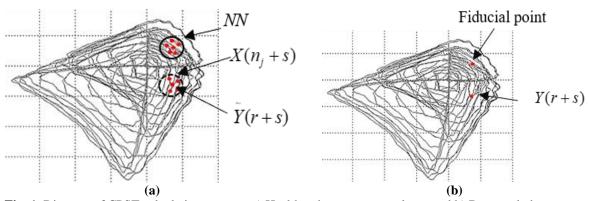


Fig. 1. Diagram of CPST calculation process: a) Healthy phase space topology; and b) Damaged phase space topology

Hence, the difference between the damage case Y and the predicted damage case \tilde{Y} of the fiducial point at time index r is determined as shown in Eq. (5) (Nie et al., 2013; Pamwani and Shelke, 2018; Tuttipongsawat et al., 2019).

$$CPST(i) = \frac{1}{P} \| \tilde{Y}(r+s) - Y(r+s) \|. \quad i$$

$$= 1. \dots nt$$
(5)

The calculation process will be repeated to obtain an average value of the *CPST* difference. The number of repetitions or fiducial points is denoted as *nt*. It is recommended to choose at least 5% of the total number of points in the reconstructed trajectory as the number of fiducial points to achieve a reasonable estimate of *CPST* (Nichols, 2003). In some references, the number of fiducial points is calculated using Eq. (6) (Nie et al., 2013).

$$nt = N - (d - 1)T \tag{6}$$

where N, d, and T: represent the total number of data points, embedding dimension, and time lag of reconstruction, respectively.

2.2.2. Mahalanobis Distance (MD)

The Mahalanobis Distance (MD) is commonly utilized to measure the distance of an individual point from a cluster of points and evaluate its deviation from the overall population. The observations of the coordinate vectors for each point from the healthy and damaged cases are represented in matrix form as [X] and [Y], respectively.

The matrices are of dimensions $(m \times d)$, where 'm' is the number of points sampled on the embedded phase portrait, equal to the number of rows. The number of columns 'd' represents the number of embedding dimensions. The healthy and damaged phase portraits are represented by two random vectors, $\{X\}$ and $\{Y\}$, respectively.

The centroid of these portraits is obtained by calculating the mean of these random vectors, denoted as $\{\mu\}_{\chi}$ and $\{\mu\}_{\gamma}$, respectively. Their covariance matrices can

also be estimated as $[C_{\chi\chi}]$ and $C_{\gamma\gamma}$, respectively. To compute the MD, a single weighted covariance matrix is derived by assigning relative weights to each of these covariance matrices. This is expressed as (George et al., 2018):

$$[C_{WW}] = W_1[C_{XX}] + W_2[C_{YY}] \tag{7}$$

The weight factors are determined based on the ratio of the number of points sampled in each phase portrait to the total number of points sampled in both. In this paper, equal weights were assigned to each covariance matrix, $W_1 = W_2 = 0.5$. The MD between the phase portraits is calculated using the following formula (George et al., 2018):

$$MD = \sqrt{(\{\mu\}_X - \{\mu\}_Y)^T [C_{WW}] (\{\mu\}_X - \{\mu\}_Y)}$$
 (8)

This modified version of the *MD* was used as a damage index in this study. More detailed information on *MD* calculation can be found in the reference (George et al., 2018).

3. Case Study

The Manavgat cable-stayed bridge, shown in Figure 2, was selected for numerical analysis. This bridge is Turkey's first cablestayed bridge, designed to accommodate two lanes of road traffic. The bridge is 202 meters long, with each span measuring 101 meters. It features a 13.7-m-wide deck connected to a steel tower by 28 cables. The tower stands approximately 42 m high and has a hollow hexagonal cross-section, mounted on a concrete foundation. The deck is constructed with a composite crosssection, comprising 25 cm of concrete, 10 cm of asphalt, and two continuous steel girders that are laterally restrained. I-shaped steel profiles are embedded continuously along the length of the deck. The deck is supported by 28 steel cables, which are interconnected with the tower. The nearest cable to the pylon is 19.6 m away, with a distance of 12 m between each subsequent cable. The last cables are situated 9.4 m from the supports. The arrangement of the cables, as well as the cross sections of the deck and the pylon, are shown in Figure 3 (Pan et al., 2018).

3.1. Finite Element Modeling

For the assessment of the structural behavior of the Manavgat cable-stayed bridge, a three-dimensional finite element model was created utilizing SAP2000 software. The deck and pylon were modeled using frame elements, and the pylon was fixed to the foundation. Truss elements were used for the cables. The details of the stay cables, labeled A1-A7 and including

14, 16, 19, 19, 22, 19, and 24 strands, respectively, are provided in Table 1 (Pan et al., 2018).



Fig. 2. Manavgat cable-stayed bridge (Elkady et al., 2023)

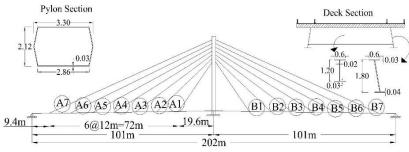


Fig. 3. Manavgat cable-stayed bridge arrangement and the cross-section of the bridge members

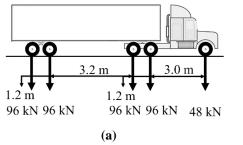
Table 1. Numbering and details of stay cables

Cable number	Cable name	Number of strands	Total area of cable (mm ²)
1	A7	24	4355
2	A6	19	3448
3	A5	22	3992
4	A4	19	3448
5	A3	19	3448
6	A2	16	2903
7	A1	15	2722
8	B1	15	2722
9	B2	16	2903
10	В3	19	3448
11	B4	19	3448
12	B5	22	3992
13	B6	19	3448
14	B7	24	4355
15	A7	24	4355
16	A6	19	3448
17	A5	22	3992
18	A4	19	3448
19	A3	19	3448
20	A2	16	2903
21	A1	15	2722
22	B1	15	2722
23	B2	16	2903
24	В3	19	3448
25	B4	19	3448
26	B5	22	3992
27	B6	19	3448
28	B7	24	4355

Each strand has an elastic modulus of 197 GPa, a cross-sectional area of 150 mm², and an ultimate strength of 1,860 MPa.

Moreover, the elastic moduli for the concrete and steel materials were specified as 34 GPa and 200 GPa, respectively. To simulate the interaction between the bridge and vehicle, examples of a five-axle and a two-axle truck, similar to the AASHTO standard load, were employed in the finite element bridge model, as illustrated in Figure 4 (Aashto, 2008). This five-axle

truck is also specified in the Australian Bridge Design Code as T44 (Australasian Railway Association, 1992). The analysis of the bridge under moving load was conducted using simulated time history analysis in the SAP2000 software. The moving load was applied to the deck through the distribution of multiple point loads at uniform intervals. Breaking down the moving load into multiple point loads and their corresponding time history function is illustrated in Figure 5.



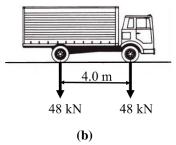


Fig. 4. Truck loadings for 3D model analysis: a) 5-axle truck (T5A); and b) 2-axle truck (T2A)

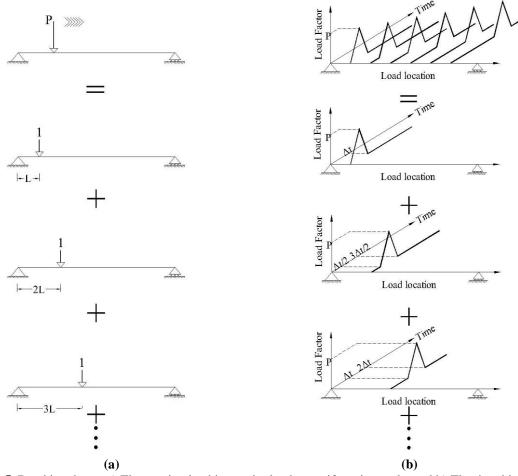


Fig. 5. Breaking down: a) The moving load into point loads at uniform intervals; and b) The time history functions

Point loads, following the load pattern depicted in Figure 5, were applied and removed from the deck. Loads were successively passed over the bridge, with Δt determined by the formula below:

$$\Delta t = \frac{L}{V} \tag{9}$$

where L: denotes the distance between point loads, while V: indicates the speed of the moving load.

4. Results and Discussion

As mentioned, the deck girder in cable-stayed bridges functions like a beam supported by elastic foundations, owing to the presence of cables. The changes in the deck's response provide crucial insights into the condition of the stay cables. In this paper, a time history analysis was performed, involving a round-trip truck at an average speed of 10-15 km/h. Dynamic effects were ignored in the analysis. The evaluation of the vertical displacement of the deck at the points of cable attachment was conducted to assess the health of the

cable-stayed bridge. The displacement of was reconstructed each point parameters of time lag and embedding dimension, extracted from the displacement vector in the phase space. To identify damaged cables through disparities in phase space trajectories between healthy and damaged cases, two distinct damage indexes were utilized: the CPST and the MD. This paper aimed to detect damage within the cables of cable-stayed bridges using two distinct loading types. comprehensive overview of methodology is outlined in the workflow depicted in Figure 6. The process of damage detection typically involves the comparison of two cases: one healthy and the other this study, damaged. In the investigation of cable damage detection was focused on five distinct cable damage scenarios under ideal conditions. The term 'ideal conditions' indicates that the passing load was consistent in both the healthy and damaged cases. The speed of the passing load was variable in the three damage scenarios. The extent of damage varied from a reduction of 10% to 45% in the cross-sectional area of the cables.

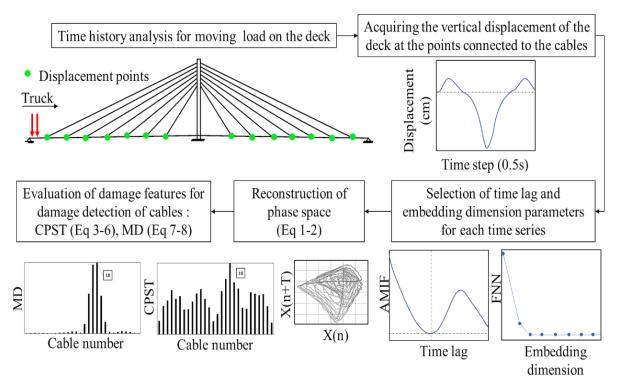


Fig. 6. Workflow of the proposed damage detection method

After reconstructing the phase space of deck displacements at the cable connection points, the two damage indices, MD and CPST, were computed and presented in Table 2. The discussion of these indices can be found in the 'damage sensitive feature' section. Except Cable 1, both MD and CPST indices (or at least one of them) accurately identified the damaged cables, namely Cables 6, 11, 18, and 25. Cable 1, which acted as a backstay cable supporting all the bridge cables, remained undetected even with a significant damage intensity of 45%.

Damage to this cable has affected all other cables. It is important to note that the index values are normalized to the highest value for ease of evaluation. Cables 1, 2, 13, 14, 15, 16, 27, and 28 were categorized as backstay cables. The damage detection

index curve for Cable 18 is illustrated in Figure 7. In this particular scenario, the speed of the passing load in the healthy case was 10 km/h, while in the damaged case, it was 15 km/h. The results were examined under a 5-axle truck (T5A). The second part the considered damage scenarios involved the passage of trucks with varying load patterns and speeds in both healthy and damaged cases. The severity of damage in these scenarios varied from 20% to 40% of the cable cross-sectional area. These scenarios were analyzed across five distinct states, as shown in Table 3. In the first state, the passing load in the healthy case was the 2-axle truck (T2A), while in the damaged case, the displacements were acquired from the passage of the 5-axle truck (T5A). The passing speed for both trucks in this state remained consistent at 10 km/h.

Table 2. Damage scenarios under ideal conditions

Cable number	Passing load (intact/damaged)	Passing speed (intact/damaged) km/h	Damage percentage (%)	Mahalanobis distance (MD)	Change in phase space topology (CPST)
1	T5A/T5A	10/10	45	26	26
6	T5A/T5A	10/10	40	5	6
11	T2A/T2A	15/15	10	11	11
18	T5A/T5A	10/15	30	18	18
25	T2A/T2A	15/10	30	25	17

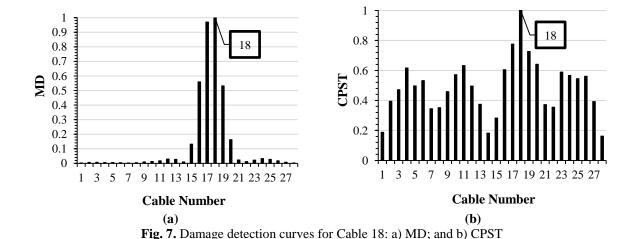


Table 3. Five states of load passing scenarios

	Intact		Damaged	
	Passing load	Passing speed km/h	Passing load	Passing speed km/h
State 1	T2A	10	T5A	10
State 2	T5A	15	T2A	10
State 3	T2A	15	T5A	10
State 4	T5A	10	T2A	15
State 5	T2A	10	T5A	15

In the second state, data were examined for the passage of the T5A truck at 15 km/h in the healthy case and the passage of the T2A truck at 10 km/h in the damaged case.

The third state was the opposite of the second one, where the trucks passing in the healthy and damaged cases changed places, but the passing speeds remained the same as

in the second state. In the fourth state, the T5A truck was used at 10 km/h in the healthy case, whereas the T2A truck was utilized at 15 km/h in the damaged case. In the fifth state, the trucks were opposite to those in the fourth state, but the passing speeds remained the same as in the fourth state.

Table 4. Results of damage detection for the damage level of 20%, excluding backstay cables

Cable number	State 1		State 2		State 3		State 4		State 5	
	MD	CPST								
3	3	3	3	25	17	16	3	12	3	17
4	3	4	4	26	17	17	3	12	4	17
5	4	18	5	25	17	18	12	12	4	5
6	5	6	26	12	17	12	12	12	5	5
7	12	3	26	11	26	17	12	12	12	3
8	25	3	3	11	12	12	17	17	9	3
٩	25	24	3	3	12	12	17	12	25	26
10	25	11	10	3	12	12	17	12	11	11
11	26	26	11	3	12	12	26	12	77	26
12	26	25	12	26	12	12	26	17	12	12
17	3	16	17	26	17	16	3	17	17	17
18	3	18	18	25	17	16	3	12	3	17
19	3	18	19	25	17	18	12	12	18	4
20	4	4	26	12	17	17	12	12	5	5
21	12	26	26	12	26	16	12	12	12	26
22	25	22	3	25	12	12	17	12	24	26
23	25	24	3	3	12	17	17	13	24	24
24	25	24	24	3	12	17	17	12	25	25
25	26	26	25	3	12	13	26	13	25	11
26	26	26	26	17	12	12	26	11	26	12

Table 5. Results of damage detection for the damage level of 30%, excluding backstay cables

Cable number	State 1		State 2		State 3		State 4		State 5	
	MD	CPST								
3	3	2	3	3	3	4	13	13	3	4
4	4	4	4	4	17	12	4	12	4	18
5	4	4	5	26	17	17	4	12	4	4
6	5	6	26	25	17	18	12	12	5	5
7	12	26	26	3	26	17	12	17	26	3
8	9	8	3	25	3	12	17	12	9	8
9	24	24	10	3	12	17	17	12	10	10
10	25	10	10	10	12	11	25	12	11	10
11	26	10	11	18	12	17	26	12	11	12
12	26	26	12	12	12	12	26	12	12	12
17	3	3	17	17	17	16	3	12	17	17
18	18	18	18	19	17	18	18	19	18	18
19	4	18	18	18	17	13	4	12	18	19
20	5	20	26	26	17	17	12	13	19	20
21	12	12	26	26	26	12	12	12	12	17
22	23	23	3	12	12	17	17	12	23	22
23	24	24	3	3	12	12	17	12	24	24
24	25	24	24	3	12	12	25	12	25	24
25	25	26	25	25	12	13	25	17	25	26
26	26	26	26	26	12	17	26	12	26	26

All cables, except for the backstay cables (totaling 20 cables), were analyzed and examined under these five states, each with three different levels of damage intensity: 20%, 30%, and 40%. The aim of examining the cables in these scenarios was to assess how well the damage detection method performs when exposed to various load patterns. The results of the damage detection indexes for cable cross-section damage levels of 20%, 30%, and 40% under the five different states are presented in Tables 4, 5, and 6, respectively. As depicted in Figure 8, to maintain uniformity in the number of data points for phase space analysis resulting from the passage of different trucks at various speeds, the arrival and departure times of the resultant load were considered.

the axles in the trucks were different, all initial data were normalized to the maximum displacement at the middle point of the bridge span. The damage indices, especially MD, accurately detected damaged cables at different levels of damage in specific cases, such as Cables 3, 12, 17, and 26. Furthermore, in several cases involving Cables 5, 10, 18, 19, 23, and 24, the MD index frequently indicated the damaged cable with a difference of one cable before or after it. However, in many cases involving cables near the pylon (Cables 7, 8, 21, and 22), the indices failed to detect the damage using this method, resulting in inconclusive outcomes. Notably, more favorable results were obtained for damage levels of 30% and higher.

Additionally, since the load values of

Table 6. Results of damage detection for the damage level of 40%, excluding backstay cables

Cable number		ite 1	State 2		State 3		State 4		State 5	
•	MD	CPST	MD	CPST	MD	CPST	MD	CPST	MD	CPST
3	3	3	3	3	17	16	3	18	3	2
4	4	3	4	4	17	16	4	12	4	4
5	4	4	4	5	4	5	4	5	4	5
6	5	6	26	12	17	12	12	12	5	6
7	12	3	26	26	26	17	12	17	26	26
8	10	10	10	15	10	18	17	12	10	9
9	24	9	10	3	12	12	17	12	10	24
10	25	10	10	10	12	11	25	12	11	10
11	11	25	11	11	12	12	25	17	11	12
12	12	12	12	12	12	12	26	17	12	26
17	17	2	17	17	17	17	3	12	17	17
18	18	17	18	18	17	12	3	18	18	17
19	4	19	19	19	17	17	4	12	18	19
20	19	20	26	25	17	18	12	16	19	20
21	12	26	26	25	26	18	12	12	26	3
22	23	22	3	27	3	12	17	17	23	22
23	24	24	23	18	12	17	17	13	24	23
24	25	24	24	10	12	11	25	12	25	25
25	25	26	25	25	12	12	25	12	25	26
26	26	26	26	26	12	13	26	13	26	13

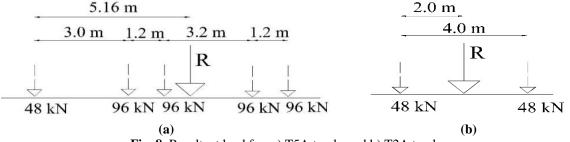


Fig. 8. Resultant load for: a) T5A truck; and b) T2A truck

The MD and CPST curves for the 40% damage level of Cables 5 and 21 are presented in Figures 9-12. The choice of Cable 5 was an example of cables for which the indexes often detected a cable before or after the damaged cable in most states.

Cable 21 was selected as one of the four

nearest cables to the pylon that could not be identified through this method. Although in cases like Cables 8 and 22 in the fifth state at damage levels of 30% and 40%, CPST correctly detected the damaged cables, it's worth noting that the accuracy of this method was limited.

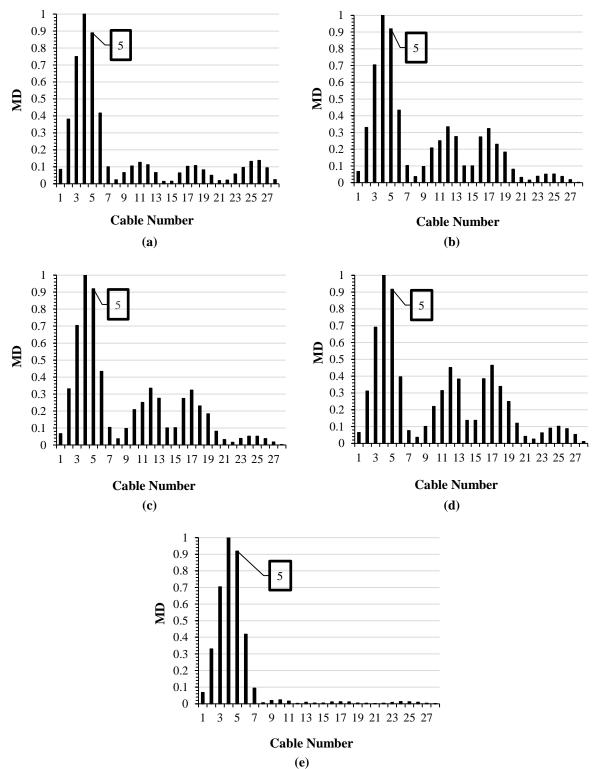


Fig. 9. MD curves of cable 5 for five states: a) State 1; b) State 2; c) State 3; d) State 4; and e) State 5

In addition, the values of the indexes in states two and five for all scenarios showed that the changes in other cables, except the damaged cable, were relatively less compared to the other states. In essence, when the T5A truck passed at a higher speed than the T2A, the changes observed in the other cables were less pronounced.

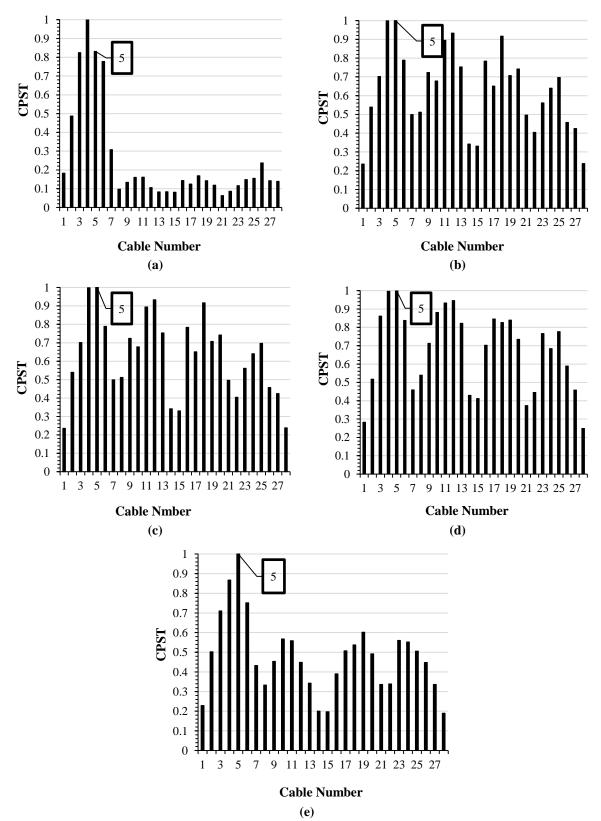


Fig. 10. CPST curves of cable 5 for five states: a) State 1; b) State 2; c) State 3; d) State 4; and e) State 5

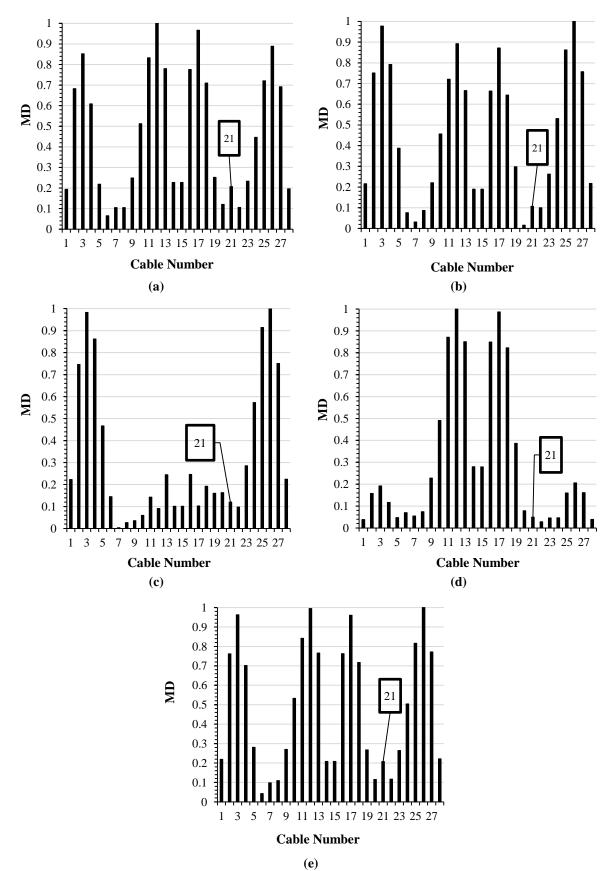


Fig. 11. MD curves of cable 21 for five states: a) State 1; b) State 2; c) State 3; d) State 4; and e) State 5

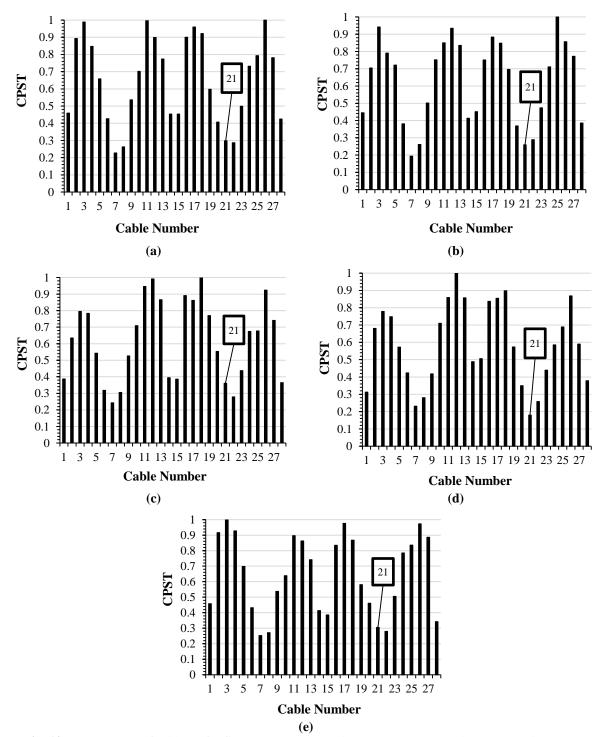


Fig. 12. CPST curves of cable 21 for five states: a) State 1; b) State 2; c) State 3; d) State 4; and e) State 5

The summary of results evaluation for MD and CPST damage indexes is presented in Table 7. Out of 100 analyses conducted, MD correctly identified 24% of scenarios when the cable damage level was 20%, while CPST correctly identified 12% of scenarios. For a damage level of 30%, these values increased to 31% for MD and 28% for CPST. When the damage level was

40%, MD and CPST indexes demonstrated the ability to detect 34% and 35% of the damaged cables across various states, respectively. Moreover, a significant percentage of the diagnoses were near the damaged cable. The MD index showed an accuracy of approximately 56%, considering both accurately and nearly detected cases for the 40% damage level.

Damage percentage	20%		30%		40%		
Damage index	MD	CPST	MD	CPST	MD	CPST	
Total number of analyses	100	100	100	100	100	100	
Exactly detected	24	12	31	28	34	35	
Nearly detected	15	14	19	20	22	12	
Accuracy	39%	26%	50%	48%	56%	47%	

Table 7. Results of damage detection for the damage level of 40%, excluding backstay cables

4.1. Comparison with Modal-Based Methods

To highlight the robustness of the phase space-based damage detection method, a comparative analysis between CPST and modal parameters was conducted. CPST derived from the displacement measurements at three distinct points on the deck, as shown in Figure 13: near the support in the first span (Point 1), adjacent to the pylon (Point 2), and in proximity to the support in the second span (Point 3). It was meticulously examined across damage levels of 10% to 50% for cable number 25 under all five aforementioned states. Modal

parameters such as the frequency of the bridge's first mode and the Modal Assurance Criterion (MAC) were analyzed. All indexes were normalized as follows (Nie et al., 2013):

$$CPST_{norm} = \frac{|CPST^d - CPST^u|}{CPST^u}$$

$$\omega_{norm} = \frac{|\omega^d - \omega^u|}{\omega^u}$$

$$MAC_{norm} = \frac{|MAC^d - MAC^u|}{MAC^u}. MAC$$

$$= \frac{\{(\varphi^u)^T \varphi^d\}^2}{\{(\varphi^u)^T \varphi^u\}\{(\varphi^d)^T \varphi^d\}}$$

$$(10-1)$$

(10-3)

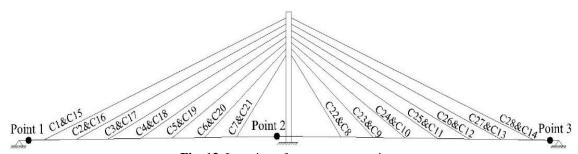
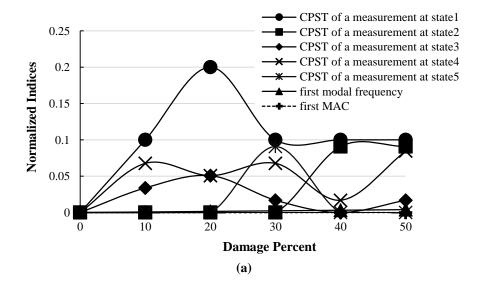


Fig. 13. Location of measurement points



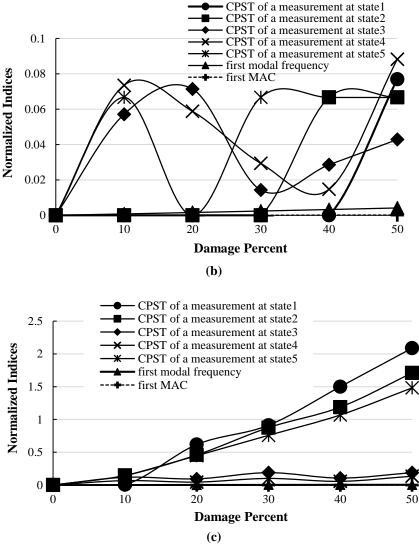


Fig. 14. A comparison of the normalized CPST and modal parameters: a) Measurement point 1; b) Measurement point 2; and c) Measurement point 3

The subscripts 'u' and 'd' denote the healthy and damaged cases, respectively. φ refers to the mode shape. Figures 14a and 14b illustrate the CPST index values and the modal parameters at Point 1 in the first span and Point 2 adjacent to the pylon. CPST exhibited heightened sensitivity to damage compared to frequency analysis. While CPST may not consistently specify the exact location of damaged cables under different load patterns and speeds, its changes were much more noticeable than those of the first mode frequency and MAC coefficient. Although they have served as significant indicators of structural damage. Figure 14c depicts the results from Point 3, which is situated near the damaged cable. Based on the previous analysis, a noticeable

correlation was observed between the CPST values and increasing damage levels across load-passing States 1, 2, and 5. For instance, at the 10% damage level, the accuracy of CPST increased by 84.5% compared to the first mode frequency of the structure across load State 1. CPST emerged as a powerful index for identifying damage in cable-stayed bridges, showcasing its robustness regardless of the location of the damage.

5. Conclusion and Future Work

A method for assessing cable health in cable-stayed bridges using phase space analysis was introduced. The proposed approach was validated through comprehensive numerical investigations conducted on the Manavgat cable-stayed bridge. The evaluation encompassed a range of scenarios, which included various loading patterns and speeds. The combination of two indices, namely the CPST and MD, was used for damage detection by identifying subtle deviations in phase space trajectories. Some important conclusions are summarized as follows:

- The damage indices accurately identified the most damaged cables in scenarios where the passing load was the same in both healthy and damaged cases. However, cables near the pylon and backstay cables presented challenges due to their interconnected role.
- The MD index displayed accuracy ranging from 39% to 56% for damage levels of 20% to 40% under various loading patterns and speeds, while the CPST index achieved accuracy between 26% and 47%. In many cases, these indexes detected cables adjacent to the damaged cable, effectively identifying the location of the damage. In states where the T5A truck passed at higher speeds, the indices demonstrated superior effectiveness.
- Some scenarios involving cables near the pylon challenged the MD and CPST in detecting damage, resulting in inconclusive responses. For damage levels of 30% and above, improved results were noted, indicating the method's heightened sensitivity to higher levels of damage.
- The comparison with modal parameters highlighted the enhanced sensitivity of CPST, derived from the phase-space response method, in detecting damage within the time domain. CPST was presented as a valuable tool for monitoring the health of cable-stayed bridges, even when the measurement point is distant from the damaged location. This paper presented an initial approach for a practical solution aimed at ensuring the health of cable-stayed exploring real-world bridges and implementations. Suggestions enhancing this method in the future include incorporating dynamic effects from highspeed loading, refining parameters with

increased precision and sensitivity (especially concerning backstay cables and those near the pylon), and considering different load placement locations within the passing lanes.

6. Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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